Structural, electronic and optical characterization of bulk platinum nitrides: a first-principles study

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We present a detailed quantum mechanical non empirical DFT investigation of the energy-optimized geometries, phase stabilities and electronic properties of bulk Pt_3N , PtN and PtN_2 in a set of twenty different crystal structures. Structural preferences for these three stoichiometries were analyzed and equilibrium structural parameters were determined. We carefully investigated the band-structure and density of states of the relatively most stable phases. Further, GW_0 calculations within the random-phase approximation (RPA) to the dielectric tensor were carried out to derive their frequency-dependent optical constants of the most likely candidates for the true crystal structure. Obtained results were comprehensively compared to previous calculations and to experimental data.

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I. INTRODUCTION

Platinum is known to form simple binary compounds with other elements (e.g. PtF_4 , PtI_2 , PtO and $PtS)^1$. However, platinum had not been known to form crystalline solid nitride, but other forms of platinum nitrides (e.g. $PtN^{1,2}$, PtN_2^1 , $(PtN)_2^{1,2}$ and Pt_2N^2) had been observed.

In January 2004, Soto³ reported the preparation of platinum thin films containing up to ~ 14 at. % nitrogen. The study concluded that platinum can form an incipient nitride phase with composition near to Pt₆N. Few months later, in May 2004, Gregoryanz and coworkers¹ published the discovery and characterization of

solid crystalline platinum mono-nitride for the first time. The synthesis was carried out above 45 GPa and 2000 K but with complete recovery of the product at room pressure and temperature. The produced samples have a very high bulk modulus leading to important implications in high-pressure physics and technology. The 1:1 stoichiometry was assigned to the new nitride, and according to their XRD measurements, Gregoryanz et al. proposed three structures: B1, B3 and B17 (for description of the structures see sub-section II A below), all based on the Pt fcc sub-lattice. Due to some considerations, B1 and B17 were ruled out and B3 was assigned to the new product.

In addition to the well-crystallized and highly ordered regions, a common feature in the synthesized platinum nitrides is the presence of sub- or/and superstoichiometric phases containing N or Pt vacancies and residual non-stoichiometric material distributed throughout the samples ^{1,4}.

The work of Gregoryanz et al. has stimulated many further theoretical studies 5-7 as expected by Gregoryanz and co-workers themselves. However, theoretical work showed that PtN(B3) is elastically and thermodynamically unstable (see sub-section III A below). Accordingly, claiming that large errors are generally inevitable in the used experimental characterization methods 6,8, and due to other paradoxical facts in the original experiment by Gregoryanz et al. theoreticians questioned the chemical stoichiometry and the crystal structure of this new material and started to investigate other possibilities 8-10. Moreover, the experimentally reported high bulk modulus of the platinum nitride has not been reproduced by any reliable calculations and its mechanism is still an unclear open problem 5,9,10.

These investigations led to a kind of consensus that the compound does not crystallize in the proposed PtN(B3) phase⁴, but the true stoichiometry and the true crystal structure have become now a matter of debate^{6,9}.

In an apparent attempt to respond to this debate, Crowhurst et al.⁴ managed, in 2006, to to reproduce and characterize platinum nitride. Combining theory with their own observed Raman spectrum, they came up with a conclusion to propose $PtN_2(C2)$ and rejected PtN(B3), proposed by the first platinum nitride synthesizers¹, and $PtN_2(C1)$, proposed in some theoretical works. Like the first proposed structures¹, $C1^8$ and $C2^4$ structures have the fcc sub-lattice of the metal.

Despite the considerable number of the subsequent theoretical studies, the discrepancy between theory and experiment in the structural and the physical properties of this nitride is not yet satisfactorily understood. Nevertheless, many transition metals can form more than one nitride¹¹. Thus, it is of interest to know if platinum can form nitrides with different stoichiometries and/or crystal structures other than those proposed by the first platinum nitride synthesizers and other researchers.

In the present work, we present a comprehensive first-principles calculations of the equation of state, possible pressure-induced phase transitions, electronic and optical properties of crystalline Pt_3N , PtN and PtN_2 in a total of twenty different -previously proposed and new hypothetical- structural modifications. The work partly aims to solve some of the reported discrepancies. In addition, to the best of our knowledge, there is no available experimental or theoretical optical data for the platinum nitride, and the present study may be the first one to calculate the optical spectra of platinum nitrides.

II. CALCULATION METHODS

A. Stoichiometries and Crystal Structures

The structure and stability of solids are influenced by their chemical stoichiometry¹² and the electronic structure of the outer shells of atoms is a controlling factor in proposing any crystal structure¹³. Like other theoretical works (cf. Table I) we postulated various structure types that are not based on the observed fcc Pt sub-lattice. Our assignment of the following different chemical stoichiometries and crystal structures is based on the fact that many transition-metal nitrides (TMNs) are known to form more than one nitride¹¹. Ni, which shares the same group with Pt, and Au which shares the same period with Pt in the periodic table, are known to form Ni₃N and Au₃N nitrides. Thus, it is of interest to consider more Pt atoms in the unit cell and less symmetric structures, and to know whether platinum can form Pt₃N with the reported structures of these and other 3:1 TMNs. In this work, the hypothetical Pt₃N is studied in the following seven structures: $D0_3$ (space group $Fm\bar{3}m$), A15 (space group Pm3n), D0₉ (space group Pm3m), L1₂ (space group Pm $\bar{3}$ m), D0₂ (space group Im $\bar{3}$), ϵ -Fe₃N (space group $P6_322$) and RhF_3 (space group $R\bar{3}c$).

The following nine structures were assigned to PtN: B1 (space group Fm $\bar{3}$ m), B2 (space group Pm $\bar{3}$ m), B3 (space group F $\bar{4}$ 3m), B8₁ (space group P6₃/mmc), B_k (space group P6₃/mmc), B_h (space group P $\bar{6}$ m2), B4 (space group P6₃mc), B17 (space group P4₂/mmc) and B24

(space group Fmmm). While C1 (space group Fm $\bar{3}$ m), C2 (space group Pa $\bar{3}$), C18 (space group Pnnm) and CoSb₂ (space group P2₁/c) are the four structures which were proposed for PtN₂.

B. Electronic Relaxation Details

As implemented in the all-electron Vienna *ab initio* Simulation Package $(VASP)^{14-19}$, our electronic structure calculations were based on spin density functional theory $(SDFT)^{20,21}$. To solve the self-consistent Kohn-Sham (KS) equations²²

$$\left\{ -\frac{\hbar^2}{2m_e} \nabla^2 + \int d\mathbf{r}' \frac{n(\mathbf{r}')}{|\mathbf{r} - \mathbf{r}'|} + V_{ext}(\mathbf{r}) + V_{xc}^{\sigma, \mathbf{k}}[n(\mathbf{r})] \right\} \psi_i^{\sigma, \mathbf{k}}(\mathbf{r}) = \epsilon_i^{\sigma, \mathbf{k}} \psi_i^{\sigma, \mathbf{k}}(\mathbf{r}), \tag{1}$$

where i, \mathbf{k} and σ are the band, \mathbf{k} -point and spin indices, respectively, the pseudo part of the KS orbitals $\psi_i^{\sigma,\mathbf{k}}(\mathbf{r})$ are expanded on plane-waves (PWs) basis. Only those PWs with kinetic energy $\frac{\hbar^2}{2m_e}|\mathbf{k}+\mathbf{G}| < E_{cut} = 600~eV$ were included. This always corresponds to changes in the total electronic energy and in the so-called Fermi energy E_F that are less than 3 meV/atom and 1 meV, respectively.

For ionic relaxation, the Brillouin zones (BZs) were sampled using $13 \times 13 \times 13$ Γ -centered Monkhorst-Pack meshes²³; while for the static calculations, $17 \times 17 \times 17$ meshes were used. Any increase in the density of this mesh corresponds to change in the total energy and in Fermi energy E_F that are less than 2 meV/atom and 0.02~eV, respectively.

Partial occupancies were set using the tetrahedron method with Blöchl corrections $^{24-26}$ for the static total energy and the electronic density of states (DOS) calculations; while in the ionic relaxation, the smearing method of Methfessel-Paxton (MP) 27 was used. In the latter case, the smearing width was set such that the fictitious entropy is always less than 1 meV/atom.

The Perdew, Burke and Ernzerhof (PBE)^{28–30} parametrization of the generalized gradient approximation (GGA)^{31–33} was employed for the exchange-correlation potentials $V_{XC}^{\sigma,\mathbf{k}}[n(\mathbf{r})]$. VASP treats the corevalence interactions, $V_{ext}(\mathbf{r})$ using the projector augmented wave (PAW) method^{19,34}. The PAW potential explicitly treats the $2s^22p^3$ electrons of N and the $5d^96s^1$ electrons of Pt as valence electrons.

In the standard mode of VASP, while fully relativistic calculations are performed for the core-electrons, only scalar kinematic effects are incorporated to treat the valance electronic structure¹⁸. It was found that this scheme is sufficient and the spin-orbit interactions have little effect on the macro-physical properties of platinum nitride⁵. Thus, we made no effort to consider spin-orbit coupling of the valence electrons.

The relaxation of the electronic degrees of freedom was performed using the blocked Davidson iteration scheme³⁵ as implemented in VASP. The electronic self-consistent (SC) convergence was considered to be achieved when the difference in the eigenvalues and in the total energy between two successive steps are both less than $1 \times 10^{-4}~eV$.

C. Geometry Optimization and EOS

At a set of isotropically varying volumes of the unit cells, ions with internal free parameters were relaxed until all Hellmann-Feynman force components on each ion were less than $1\times 10^{-2}~eV/\text{Å}$. Static total energy calculations (as described above) at each volume followed and the cohesive energy per atom was calculated from 37,38

$$E_{coh}^{\mathrm{Pt}_{m}\mathrm{N}_{n}} = \frac{E_{\mathrm{solid}}^{\mathrm{Pt}_{m}\mathrm{N}_{n}} - Z \times \left(mE_{\mathrm{atom}}^{\mathrm{Pt}} + nE_{\mathrm{atom}}^{\mathrm{N}}\right)}{Z \times (m+n)}. \quad (2)$$

Here, Z is the number of $\operatorname{Pt}_m \mathcal{N}_n$ per unit cell, $E_{\mathrm{atom}}^{\operatorname{Pt}}$ and $E_{\mathrm{atom}}^{\operatorname{N}}$ are the energies of the spin-polarized non-spherical isolated Pt and N atoms, $E_{\mathrm{solid}}^{\operatorname{Pt}_m \mathcal{N}_n}$ are the bulk cohesive energies calculated by VASP with respect to spherical non spin-polarized reference atoms, and m, n = 1, 2 or 3 are the stoichiometric weights.

The calculated E_{coh} per atom as a function of volume V per atom were fitted to a Birch-Murnaghan 3rd-order equation of state (EOS)³⁹

$$E(V) = E_0 + \frac{9V_0B_0}{16} \left(\left[\left(\frac{V_0}{V} \right)^{\frac{2}{3}} - 1 \right]^3 B_0' + \left[\left(\frac{V_0}{V} \right)^{\frac{2}{3}} - 1 \right]^2 \left[6 - 4 \left(\frac{V_0}{V} \right)^{\frac{2}{3}} \right] \right).$$
(3)

The four equilibrium fitting parameters: the equilibrium volume V_0 , the equilibrium cohesive energy E_0 , the equilibrium bulk modulus

$$B_0 = -V \frac{\partial P}{\partial V}\Big|_{V = V_0} = -V \frac{\partial^2 E}{\partial V^2}\Big|_{V = V_0} \tag{4}$$

and its pressure derivative

$$B_0' = \frac{\partial B}{\partial P}\Big|_{P=0} = \frac{1}{B_0} \left(V \frac{\partial}{\partial V} (V \frac{\partial^2 E}{\partial V^2}) \right) \Big|_{V=V_0} \tag{5}$$

were determined by a least-squares method.

D. Formation Energy

In addition to $E_{\rm coh}$, another important measure of relative stability is the so-called formation energy E_f . Assuming that the solid ${\rm Pt}_m{\rm N}_n$ results from the interaction between the solid ${\rm Pt}(fcc)$ metal and the gaseous ${\rm N}_2$ through the chemical reaction

$$m\mathrm{Pt}^{\mathrm{solid}} + \frac{n}{2}\mathrm{N}_{2}^{\mathrm{gas}} \rightleftharpoons \mathrm{Pt}_{m}\mathrm{N}_{n}^{\mathrm{solid}},$$
 (6)

 E_f can be obtained from

$$E_f(\operatorname{Pt}_m \operatorname{N}_n^{\text{solid}}) = E_{\text{coh}}(\operatorname{Pt}_m \operatorname{N}_n^{\text{solid}}) - \frac{mE_{\text{coh}}(\operatorname{Pt}^{\text{solid}}) + \frac{n}{2}E_{\text{coh}}(\operatorname{N}_2^{\text{gas}})}{m+n} . \quad (7)$$

where m,n=1,2,3 are the stoichiometric weights and $E_{\rm coh}({\rm Pt}_m{\rm N}_n^{\rm solid})$ is the cohesive energy per atom as obtained from Eq. 2. The ground-state cohesive energy and other equilibrium properties of the elemental platinum $E_{\rm coh}({\rm Pt}^{\rm solid})$ in its fcc A1 structure (space group Fm3m No. 225) $^{40-42}$ are given in Table I. We found the equilibrium cohesive energy of the molecular nitrogen $(E_{\rm coh}({\rm N}_2^{\rm gas}))$ and its N–N bond length to be $-5.196~eV/{\rm atom}$ and 1.113 Å. For details on how these properties were calculated, readers are referred to Ref. 43.

E. GWA Calculations and Optical Properties

Accurate quantitative description of optical properties of materials requires treatments beyond the level of DFT⁴⁴. One choice is to follow the method which is provided by the many-body perturbation theory (MBPT). In this approach one needs to solve a system of quasiparticle (QP) equations $^{45-47}$

$$\left\{ -\frac{\hbar^{2}}{2m} \nabla^{2} + \int d\mathbf{r}' \frac{n(\mathbf{r}')}{|\mathbf{r} - \mathbf{r}'|} + V_{ext}(\mathbf{r}) \right\} \psi_{i,\mathbf{k}}^{QP}(\mathbf{r})
+ \int d\mathbf{r}' \Sigma(\mathbf{r}, \mathbf{r}'; \epsilon_{i,\mathbf{k}}^{QP}) \psi_{i,\mathbf{k}}^{QP}(\mathbf{r}') = \epsilon_{i,\mathbf{k}}^{QP} \psi_{i,\mathbf{k}}^{QP}(\mathbf{r}).$$
(8)

In practice, one takes the wave functions $\psi_{i,\mathbf{k}}^{QP}(\mathbf{r})$ from the DFT calculations. However, this technique is computationally expensive, and we had to use less dense meshes of **k**-points: $(10\times10\times10)$ in the case of B17 and $(12\times12\times12)$ in the case of B3. The quantity $\Sigma(\mathbf{r},\mathbf{r}';\epsilon_{i,\mathbf{k}}^{QP})$ in Eqs. 8 above is known as self-energy. It contains all the static and dynamic exchange and correlation effects, including those neglected at the DFT-GGA level. When Σ is written in terms of the Green's function G and the frequency-dependent screened Coulomb interaction W as

$$\Sigma_{GW} = j \int d\epsilon' G(\mathbf{r}, \mathbf{r}'; \epsilon, \epsilon') W(\mathbf{r}, \mathbf{r}'; \epsilon), \qquad (9)$$

the approximation is referred to as GW approximation. The dynamically screened interaction W is related to the bare interaction v via

$$W(\mathbf{r}, \mathbf{r}'; \epsilon) = j \int d\mathbf{r}_1 \varepsilon^{-1}(\mathbf{r}, \mathbf{r}_1; \epsilon) v(\mathbf{r}_1, \mathbf{r}'), \quad (10)$$

where the dielectric matrix ε is calculated within the random phase approximation (RPA). The QP eigenvalues

$$\epsilon_{i,\mathbf{k}}^{QP} = \operatorname{Re}\left(\left\langle \psi_{i,\mathbf{k}}^{QP} \middle| H_{KS} - V_{XC} + \Sigma_{GW_0} \middle| \psi_{i,\mathbf{k}}^{QP} \right\rangle\right) (11)$$

are updated in the calculations of G, while W is kept at the DFT-RPA level. This is called the GW_0 self-consistent routine on G. After the execution of the fourth iteration, ε is recalculated within the RPA using the updated QP eigenvalues^{46–48}. It is straightforward then to calculate all the frequency-dependent optical spectra (e. g. refractive index $n(\omega)$, extinction coefficient $\kappa(\omega)$, absorption coefficient $\alpha(\omega)$, reflectivity $R(\omega)$ and transmitivity $T(\omega) = 1 - R(\omega)$) from the real $\varepsilon_{\rm re}(\omega)$ and the imaginary $\varepsilon_{\rm im}(\omega)$ parts of $\varepsilon_{\rm RPA}(\omega)^{49-51}$:

$$n(\omega) = \frac{1}{\sqrt{2}} \left(\left[\varepsilon_{\rm re}^2(\omega) + \varepsilon_{\rm im}^2(\omega) \right]^{\frac{1}{2}} + \varepsilon_{\rm re}(\omega) \right)^{\frac{1}{2}}$$
 (12)

$$\kappa\left(\omega\right) = \frac{1}{\sqrt{2}} \left(\left[\varepsilon_{\rm re}^2\left(\omega\right) + \varepsilon_{\rm im}^2\left(\omega\right) \right]^{\frac{1}{2}} - \varepsilon_{\rm re}\left(\omega\right) \right)^{\frac{1}{2}}$$
 (13)

$$\alpha(\omega) = \sqrt{2\omega} \left(\left[\varepsilon_{\rm re}^2(\omega) + \varepsilon_{\rm im}^2(\omega) \right]^{\frac{1}{2}} - \varepsilon_{\rm re}(\omega) \right)^{\frac{1}{2}}$$
 (14)

$$R(\omega) = \left| \frac{\left[\varepsilon_{\text{re}} \left(\omega \right) + j \varepsilon_{\text{im}} \left(\omega \right) \right]^{\frac{1}{2}} - 1}{\left[\varepsilon_{\text{re}} \left(\omega \right) + j \varepsilon_{\text{im}} \left(\omega \right) \right]^{\frac{1}{2}} + 1} \right|^{2}$$
(15)

It may be worth to emphasize here that for more accurate optical properties (e.g. more accurate amplitudes and positions of the characteristic peaks), electron-hole excitations should be calculated by solving the so-called Bethe-Salpeter equation, the equation of motion of the two-body Green function G_2 . The latter can be evaluated on the basis of our obtained GW one-particle Green function G and QP energies⁵².

III. RESULTS AND DISCUSSION

Cohesive energy $E_{\rm coh}$ versus atomic volume V_0 equation of state (EOS) for the different phases of Pt₃N, PtN₂ and PtN are displayed graphically in Fig. 1, Fig. 2 and Fig. 3, respectively. The corresponding obtained equilibrium structural parameters and energetic and elastic properties are presented in Table I. In this table, as well as in Fig. 4, structures are first grouped according to the nitrogen content, starting with the stoichiometry with the lowest nitrogen content Pt₃N, followed by the 1:1 series and ending with the nitrogen-richest PtN₂ group. Within each series, structures are ordered according to their structural symmetry, starting from the highest symmetry (i.e. the highest space group number) to the least symmetry. Whenever possible, our results are compared with experiment and with previous calculations. In the latter case, the calculations methods and the XC functionals are indicated in the Table footnotes.

To study the effect of nitridation on the elemental Pt(A1) and to easly compare the properties of these phases relative to each other, the calculated equilibrium properties are displayed relative to the corresponding ones of Pt(A1) in Fig. 4.

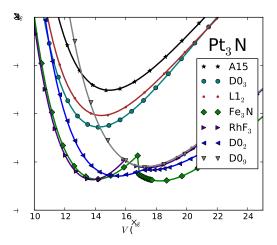


FIG. 1. (Color online.) Cohesive energy $E_{\rm coh}(eV/{\rm atom})$ versus atomic volume V (Å³/atom) for Pt₃N in seven different structural phases.

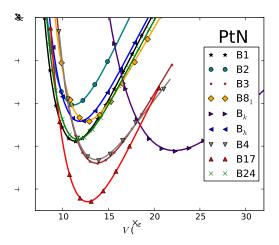


FIG. 2. (Color online.) Cohesive energy $E_{\rm coh}(eV/{\rm atom})$ versus atomic volume V (ų/atom) for PtN in nine different structural phases.

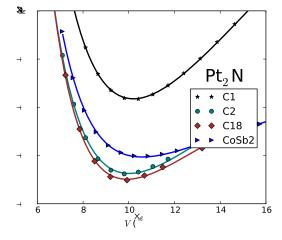


FIG. 3. (Color online.) Cohesive energy $E_{coh}(eV/\text{atom})$ versus atomic volume $V(\mathring{A}^3/\text{atom})$ for PtN₂ in four different structural phases.

TABLE I. The calculated (Pres.) zero-pressure properties of the platinum nitrides and the results of previous calculations (Comp.). The available experimental data are given in the last row.

		$a(\mathring{A})$	$b(\mathring{A})$	$c(\mathring{A})$	$\alpha(^{\circ}) \text{ or } \beta(^{\circ})$	$V_0(\text{Å}^3/\text{atom})$	$E_{\rm coh}(eV/{\rm atom})$	$B_0(GPa)$	B_0'	$E_f(eV/atom)$
						Pt				
	Pres.	3.978	_	_	_	15.74	-5.451	242.999	5.486	
A1	E4	$(3.9233 \pm 0.0007)^{a}$	_	_	_	15.097 ^b	-5.84^{c}	278.3°, 280 ^d	5.18 ^e	
	Expt.	3.924 ^{ee}	_	_	_			249 ^{ee}	5.23 ^{ee}	
	Comp.	$3.90^{\rm g}, 3.890^{\rm s}, 3.981^{\rm gg},$	_	_	_		$-7.04^{\rm h}, -3.74^{\rm i},$	305 ^g , 320 ^s , 238 ^t	5.16 ^k , 5.30 ^l , 5.25 ^m	
	Comp.	3.967 ^t , 3.966 ^{cc}	_	_	_		-5.53^{j}	249 ^{cc} , 242 ^{dd} , 244.18 ^{gg}	5.23 ^{cc} , 5.83 ^{dd} , 5.7 ^{gg}	
						Pt_3N	I			
$D0_3$	Pres.	6.106	-	-	-	14.23	-4.140	218.097	5.282	1.247
A15	Pres.	4.924	-	-	_	14.92	-3.759	194.136	5.266	1.628
$\mathbf{D0}_{9}$	Pres.	4.114	_	_	_	17.41	-4.558	167.839	5.241	0.829
$\mathbf{L}1_2$	Pres.	3.863	-	-	_	14.41	-4.021	205.279	5.472	1.366
$\mathbf{D0}_2$	Pres.	7.875	_	_	_	15.26	-4.644	147.174	12.098	0.743
ϵ -Fe ₃ N		5.680	_	5.293	_	18.49	-4.713	217.035	6.779	0.674
\mathbf{RhF}_3	Pres.	5.463	_	_	$\alpha = 58.640$	13.97	-4.688	224.419	5.412	0.699
	_					PtN				
	Pres.	4.495	-	-	_	11.35	-3.945	230.869	5.059	1.378
B1		4.45^{x} , 4.50^{y} , 4.41^{z}	-	-	_	er.		232 ^x , 230 ^y , 288 ^z		
	Comp.	4.471 ^{cc}	-	-	_	10.66 ^{ff}		251 ^{cc} , 242 ^{dd} , 294 ^{ff}	4.00°c, 4.78°dd	1.365 ^{cc}
	_	4.491 ^{gg}	_	_	_			229.76^{gg}	4.9 ^{gg}	$[0.375 + E_f(B17)]^{hl}$
B2	Pres.	2.819	-	-	_	11.20	-3.522	238.187	5.070	1.801
	Comp.	2.818 ^{gg}	_	_	_			234.88 ^{gg}	5.1 ^{gg}	
В3	Pres.	4.782	-	-	_	13.67	-4.203	193.466	5.031	1.120
		4.7217 ⁿ , 4.8250°, 4.779 ^{gg} ,	-	_	_			243.3°, 196.3°, 190.61 ^{gg} ,	5.100,	0.0588
	Comp.	4.6833 ^p , 4.7889 ^q , 4.8114 ^r ,	_	_	_			271.9 ^p , 192.7 ^q , 184 ^r ,	4.00 ^{cc}	0.95 ^{aa} 1.1 ^{cc}
		4.692 ^s , 4.780 ^t , 4.760 ^{cc} ,	_	_	_			244 ^s , 194 ^t , 213 ^{cc} ,	3.62 ^{dd}	and the second s
De	Pres.	4.80 ^{x,y} , 4.70 ^z , 4.699 ^{hh} 3.482	_	4.843		12.71	-3.713	192 ^x , 190 ^y , 232 ^z , 217 ^{dd} 210.165	4.945	$[0.21 + E_f(B17)]^{hh}$ 1.610
$\frac{\mathrm{B8_1}}{\mathrm{B_k}}$	Pres.	3.378		8.986		22.20	-3.713 -4.061	108.968	4.553	1.010
$\frac{B_k}{B_h}$	Pres.	3.039		2.966		11.86	-4.061 -3.716	222.279	5.014	1.607
	Pres.	3.382	_	5.539	_	13.72	-3.710 -4.171	190.130	5.033	1.152
B4	Comp.	3.386 ^{gg}	_	5.529 ^{gg}		13.72	-4.171	191.06 ^{gg}	4.7 ^{gg}	1.102
	Pres.	3.069		5.403		12.72	-4.652	235.041	5.018	0.671
B17	Comp.	3.323 ^{hh}	_	4.579 ^{hh}		12.12	-4.052	255.041	5.016	0.071
	Pres.	4.216	4.472	4.948	_	11.66	-3.928	226.608	5.153	1.395
B24		3.972 ^{hh}	3.977 ^{hh}			11.00	-3.320	270 ^{hh}	0.100	$[0.085 + E_f(B17)]^{hl}$
	Comp.	3.912	3.311	0.022		PtN		210		$[0.005 + E_f(D11)]$
	Pres.	4.963	_	_	_	10.19	-3.918	263.295	4.717	1.363
C1		4.9428 ⁿ , 5.0403°,	_	_	_	10.10	0.010	322.1 ⁿ , 267.2°, 269 ^{cc} ,	4.00 ^{cc}	1.167 ^{aa}
	Comp.	4.866 ^s , 4.958 ^t , 4.939 ^{dd}	_	_	_			316 ^s , 264 ^t , 260 ^{dd}	4.73 ^{dd}	1.317 ^{dd}
	Pres.	4.912	_	_	_	9.882	-4.689	226.779	6.893	0.592
C2		4.87 ^{aa}	_	_	_	9.12 ^{ff}				0.267 ^{aa} , 0.24 ^{bb}
	Comp.	4.848 ^{cc} , 4.874 ⁱⁱ	_	_	_	9.65 ⁱⁱ		305 ^{cc} , 285 ^{dd} , 300 ⁱⁱ	4.00°c, 5.50°dd	0.64 ^{cc} , 0.212 ⁱⁱ
C18	Pres.	3.036	3.984	4.862	_	9.800	-4.755	244.320	7.938	0.526
	Comp.	3.778 ⁱⁱ	4.880 ⁱⁱ	3.208 ⁱⁱ	_	9.827 ⁱⁱ	1.100	286 ⁱⁱ		0.249 ⁱⁱ
	Pres.	5.460	5.163	9.374	$\beta = 151.225$		-4.508	118.594	6.619	0.773
\mathbf{CoSb}_2	Comp.	4.950 ⁱⁱ	4.880 ⁱⁱ	4.950 ⁱⁱ	$\beta = 151.225$ 99.50^{ii}	9.827 ⁱⁱ	1.000	289 ⁱⁱ	0.010	0.248 ⁱⁱ
	Jonep.	1.000	4.000	4.000	55.50	Experin	nent.	200		0.240
		$(4.8032 \pm 5)^{\mathrm{u,v}}, 4.8041(2)^{\mathrm{w}}$	_	_	_	Experm		$(372 \pm 5)^{\mathrm{u}}, (354 \pm 5)^{\mathrm{v}}$	4.0 ^u , 5.26 ^v	
		(1.0002 ± 0) , 4.0041(2)						(0.2 ± 0) , (00± ± 0)	1.0 , 0.20	

^a Ref. 53: This is an average of 23 experimental values, at room temperature.

^b Ref. 53: at room temperature.

^c Ref. 54: Cohesive energies are given at 0 K and 1 atm = 0.00010 GPa; while bulk moduli are given at room temperature.

^d Ref. (25) in 55: at room temperature.

^e See Refs. (8)–(11) in 55.

g Ref. 56: using the full-potential linearized augmented plane waves (LAPW) method within LDA.

^h Ref. 57: using the projector augmented wave (PAW) method within LDA.

ⁱ Ref. 57: using the projector augmented wave (PAW) method within GGA(PW91).

^j Ref. 57: using the projector augmented wave (PAW) method within GGA(PBE).

k Ref. 55: using the so-called method of transition metal pseudopotential theory; a modified form of a method proposed by Wills and Harrison to represent the effective interatomic interaction.

¹ Ref. 55: using a semi-empirical estimate based on the calculation of the slope of the shock velocity vs. particle velocity curves

obtained from the dynamic high-pressure experiments. The given values are estimated at $\sim 298~K$. ^m Ref. 55: using a semi-empirical method in which the experimental static P-V data are fitted to an EOS form. The given values are estimated at $\sim 298 K$.

ⁿ Ref. 5: using the ultrasoft pseudopotential (USPP) method within LDA. B₀'s are calculated from elastic constants.

^o Ref. 5: using the ultrasoft pseudopotential (USPP) method within GGA. B_0 's are calculated from elastic constants.

^p Ref. 5: using the projector augmented wave (PAW) method within LDA. B'_0 is set to be 4.

^q Ref. 5: using the projector augmented wave (PAW) method within GGA. B'_0 is set to be 4.

^r Ref. 5: using fully relativistic full-potential linearized augmented plane waves (LAPW) method within GGA.

^s Ref. 8: using the full-potential linearized augmented plane waves (LAPW) method within LDA.

^t Ref. 8: using the full-potential linearized augmented plane waves (LAPW) method within GGA(PBE).

^u Ref. 1: The experimental evolution of the volume with pressure was fitted with a Birch-Murnaghan EOS, but B'_0 was set to be 4. ^v Ref. 1: The experimental evolution of the volume with pressure was fitted with a Birch-Murnaghan EOS, but $B'_{0,Pt} = 5.26$ was fixed.

 $^{^{\}mathrm{w}}$ Ref. 1: From XRD measurements at 0.1 MPa.

x Ref. 9: using the full-potential linearized augmented plane waves (FPLAPW) method within GGA(PBE).

y Ref. 9: using pseudopotentials method within GGA(PBE).

^z Ref. 9: using pseudopotentials method within LDA.

^{aa} Ref. 4: using the PAW method within GGA(PW91), but the experimental value of $E_{\rm coh}(N_2^{\rm gas})$ in Eq. 7 was used.

bb Ref. 4: using the full-potential linear-augmented plane-wave method.

cc Ref. 6: using pseudopotentials method within GGA(PBE).

^{dd} Ref. 6: using pseudopotentials method within GGA(PBE).

ee Ref. 58.

ff Ref. 7: using the pseudopotential method within LDA.

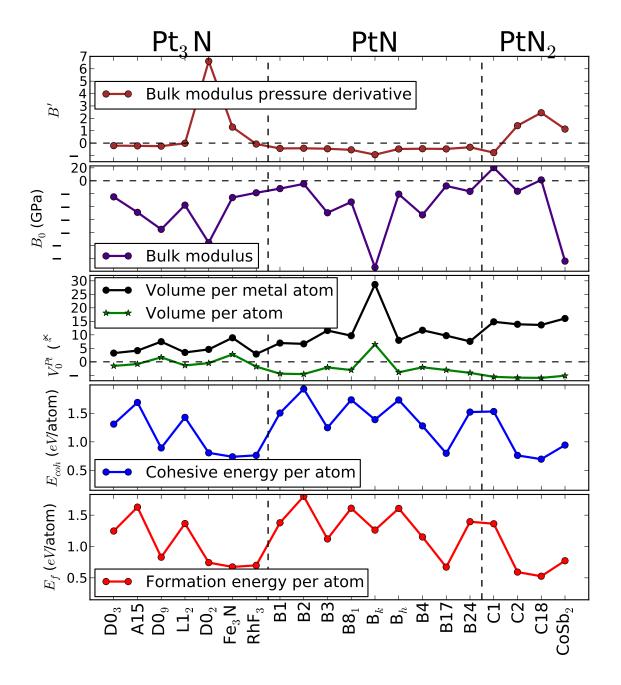


FIG. 4. (Color online.) Calculated equilibrium properties of the twenty studied phases of platinum nitrides. All quantities are given relative to the corresponding ones of the fcc crystalline elemental platinum given in the first row of Table I.

A. EOS and Relative Stabilities

Fig. 1 reveals that Pt₃N in its least symmetric phase, the trigonal (rhombohedric) structure of RhF₃, is the most favorable phase in this series. However, after $\sim 15.9 \ \text{Å}^3/\text{atom}$ the EOS of Pt₃N(RhF₃) is almost identical with the EOS of Pt₃N in the simple cubic structure of the anti-ReO₃ (D0₉). They share a minimum at $\sim (17.4 \ \text{Å}^3/\text{atom}, -4.56 \ eV)$. Very close to this point, at $\sim (17.23 \ \text{Å}^3/\text{atom}, -4.59 \ eV)$, the EOS of Pt₃N(D0₂) has a kink due to a change in the positions of some Pt ions.

The EOS of $\operatorname{Pt}_3N(\operatorname{Fe}_3N)$ has two minima located at $(14.11 \ \mathring{A}^3/\operatorname{atom}, -4.697 \ eV)$ and $(18.26 \ \mathring{A}^3/\operatorname{atom}, -4.679 \ eV)$. Thus, the two minima are very close in energy but, due to the difference in V_0 , they correspond to bulk moduli of 222.7 GP and 169.0 GP, respectively. The Pt ions are in the 6g Wyckoff positions: $(x,0,0),(0,x,0),(-x,-x,0),(-x,0,\frac{1}{2}),(0,-x,\frac{1}{2})$ and $(x,x,\frac{1}{2})$. Upon ion relaxation of $\operatorname{Pt}_3N(\operatorname{Fe}_3N)$, atomic positions change from $x\sim\frac{1}{3}$ to $x=\frac{1}{2}$ causing the sudden change in the potential surface (at $\sim 16.83 \ \mathring{A}^3/\operatorname{atom}$) as the bulk $\operatorname{Pt}_3N(\operatorname{Fe}_3N)$ being decompressed (Fig. 1). It may be worth mentioning here that $\operatorname{Ag}_3N(\operatorname{Fe}_3N)^{61}$ and $\operatorname{Cu}_3N(\operatorname{Fe}_3N)^{43}$ were found to behave in a similar manner.

Hence, one of the two minima in the EOS of $Pt_3N(RhF_3)$ is shared with the minimum of the EOS of $Pt_3N(D0_9)$ and the other is shared with one of the two minima of $Pt_3N(Fe_3N)$.

The crossings of the less stable $D0_3$, $L1_2$ and A15 EOS curves with the more stable $D0_9$ EOS at the left side of their equilibria indicates that $D0_9$ would not survive under pressure and that possible pressure-induces phase transitions from the latter phase to the former ones may occur.

Fig. 4 shows that the Pt_3N most stable phases may energetically compete with the PtN and PtN_2 most stable ones. However, from the foregoing discussion, it seems that Pt_3N would not have a simple potential surface.

Using the full potential augmented plane wave plus local orbitals (APW+lo) method within GGA(PBE), the energy-volume EOS's for B1, B2, B3 and B4 have been studied by the authors of Ref. 59. Some of their obtained equilibrium properties are included and referred to in Table I. Within the considered parameter sub-space, our obtained EOS's (Fig. 2), relative stabilities, and equilibrium structural parameters and mechanical properties (Table I) are in excellent agreement with their findings. However, relaxing the c/a parameter, they obtained an additional EOS which lies below all the other considered ones, but its equilibrium B_0 is significantly smaller.

From Fig. 2, it is evident that PtN(B17) is the energetically most stable phase in the PtN series. The differ-

ence in the equilibrium $E_{\rm coh}$ between PtN(B17) and the next (less) stable phase, PtN(B3), is about 0.5 eV (Table I). This difference was found by other researchers⁹ to be 0.9-1.05~eV. The crossings of the EOS curve of B17 with some of those of less stability at the left side of their equilibria reveals possible pressure-induces phase transitions. To closely investigate these transitions, we plot the corresponding relations between enthalpy H = E(V) + PVand the imposed external pressure P. Possible transitions and the pressures at which they occur are carefully depicted. A point where two H(P) curves (of two modifications with the same chemical stoichiometry⁷) meet represents a phase transition from the phase with the higher H to the one with the lower H^{37} . From the H(P) diagrams (not shown here) we found that PtN(B17) would transform to PtN(B1, B2, B_h or B24) at \sim 93 GPa, ~ 143 GPa, ~ 193 GPa or ~ 123 GPa, respectively.

It may be worth to mention here a few points about this B17 structure: (i) It was theoretically predicted to be the ground-state structure of CuN^{43} , AgN^{61} , AuN^{62} and PdN^{63} . (ii) The same foregoing phase PtN-PtN structural pressure-induced transitions have been predicted for PdN, but at relatively smaller pressures in the range $(25.8 \sim 62.1 \text{ GPa})^{63}$. (iii) B17 is the structure of PtS⁶⁴ and PtO⁹. (iv) It was found by other authors to be a possible ground state for PtN⁹. (v) The B17 structure has an fcc Pt sub-lattice (as the synthesized platinum nitride), but it is tetragonal and the sub-lattice are highly distorted $(c/a \approx \sqrt{3} \text{ versus } c/a = \sqrt{2} \text{ for ideal fcc)}$, and probably because of this distortion it was rejected by the platinum nitride synthesizers¹. (vi) Fig. 5 that B17 is energetically favorable over B1 and B3 at all pressures.

Nevertheless, PtN(B17) was found to be elastically unstable 10 .

Assuming 1:1 stoichiometry, the first platinum nitride synthesizers assigned the B3 structure for their product 1 . However, it was shown in the same work that PtN(B3) should break down or transform at pressures above 12 GPa. In agreement with this experimental prediction, Fig. 5 shows that PtN(B3) would not survive at pressures above 19 GPa where the B3 \rightarrow B1 phase transition occurs. Other theoretical works also predicted that B1 becomes more favorable than B3 structure above $13.3~{\rm GPa}^9, \sim 15~{\rm GPa}^7, 16.5~{\rm GPa}^9,$ and $17.6~{\rm GPa}^9.$

Therefore, we support Ref. 9 on the judgment that, unless the PtN(B3) was formed upon depressurization, its production at $45-50~\mathrm{GPa^1}$ is questioned. Further, first-principles calculations showed that PtN(B3) is elastically unstable^{5,6,8}, and that it may distort spontaneously to a tetragonal lattice to lower the energy⁸.

In the PtN_2 series, we can see from Table I and from Fig. 4 that PtN_2 in the simple orthorhombic structure of FeS_2 marcasite (C18) is the most stable phase, while the face-centered cubic structure of CaF_2 fluorite (C1) is significantly the least favorable structure. Yet, Fig. 5 reveals that the latter $PtN_2(C1)$ is more favorable than the proposed PtN(B1, B3 and B17) at pressures above

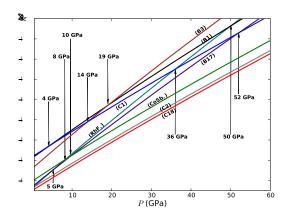


FIG. 5. (Color online.) Enthalpy H vs. pressure P equation of state (EOS) for the most favorable Pt_3N phase (RhF₃), the three proposed PtN modifications (B1, B3 and B17), and the four considered PtN_2 structures in the present work (C1, C2, C18 and $CoSb_2$). The arrows indicate the pressures at which curves cross each other.

4 GPa, 14 GPa and 52 GPa, respectively. Others⁹ found $PtN_2(C1)$ to be more favorable than PtN(B3) at pressures above 30 GPa.

In contrast to our enthalpy-pressure EOS's in Fig. 5, Chen, Tse and Jiang⁶⁰ obtained an H(P) curve for C18 which lies always above the curve for C2 and coincides with the one of CoSb₂. They concluded that C2 is the most stable structure among these three modifications. While we sticked to the original C18 relative dimensions, it seems that Chen, Tse and Jiang tried to optimize the lattice parameters ratios (see Table I). However, the c:a:b ratio they obtained is very close to our a:b:c ratio, and the difference in V_0 is less than 0.03 Å³/atom)⁶⁵. Another difference is the atomic electronic configuration of Pt $5d^86s^2$ they used. Nevertheless, they agreed with us that in the 0-60 GPa pressure range, no transition between these three phases occurs.

Comparing the relative stability of the three most stable compositions, we find from Table I and from Fig. 4 that $PtN_2(C18)$ is the most favorable, followed by $Pt_3N(RhF_3)$, and the least stable phase is PtN(B17). However, the differences in their equilibrium E_{coh} lies within a narrow range of 0.036 eV. Relative to their parent metal, all phases have higher E_{coh} , i.e. they are less bound than Pt(A1). Hence, we found, as other theoretical works⁸, that platinum nitride can be stabilized in stoichiometries and structures other than that proposed by the first synthesizers¹.

In Ref. 9, the energy-volume EOS for B1, B3, B17, C1, and C2 have been studied using DFT-GGA. Within this parameter sub-space, our obtained EOS's (Figs. 2, 3 and 4) are in excellent agreement with the findings of 9. From the relative enthalpy-pressure diagrams⁶⁶, Ref. 9 arrived at an astonishing result: the experimentally

proposed PtN(B3) is an entirely unstable structure at any pressure.

To closely study the non-zero pressure stoichiometric and structural preferences, we displayed in Fig. 5 the enthalpy H vs. pressure P equation of states (EOS) for the most favorable Pt₃N phase (RhF₃), the three previously proposed PtN modifications (B1, B3 and B17), and the four considered PtN₂ structures in the present work (C1, C2, C18 and CoSb₂). The arrows indicate the pressures at which curves cross each other. From these curves, it is clear that PtN₂(C18), followed by $PtN_2(C2)$, are the most energetically favorable phases at all pressure. At pressures above 10 GPa, PtN₂(CoSb₂) has lower enthalpy than the rest of the modifications, including PtN(B17) and PtN₂(C1). At pressures higher than 8 GPa, PtN(B17) becomes more favorable than Pt₃N(RhF₃), but the former never competes behind 52 GPa when PtN₂(C1) becomes more favorable. However, Pt₃N(RhF₃) is more stable than PtN(B3) at all pressures. In summary, Fig. 5 reveals that even if a PtN phase has been observed (at pressures around 50 GPa), this phase must be unstable toward phase decomposition into solid constituents Pt and PtN₂ (see also Ref. 7) or into Pt and Pt₃N. However, the series of the possible phase transitions must be carefully investigated.

B. Volume per Atom and Lattice Parameters

The obtained equilibrium volume per atom V_0 , i.e. the inverse of the number density, for all the considered modifications are numerally presented in Table I and graphically depicted relative to the Pt(A1) in Fig. 4. On average, Pt_3N phases tend not to change the number density of the host parent Pt(A1); PtN phases tend to slightly increase it; while the PtN_2 increase it significantly.

It is also evident from Fig. 4 that in crossing the boarders between the Pt₃N and PtN and between the PtN and PtN₂ islands, i.e. in increasing the N content, V_0 tends to decrease while the volume per Pt atom $V_0^{\rm Pt}$, a measure of the average Pt–Pt bond length, tends to increase. The latter finding has been found to be true for the nitrides of Cu⁴³ and Ag⁶¹ as well.

C. Bulk Modulus and its Pressure Derivative

With only a few exceptions, Fig. 4 and Table I reveal that nitridation of Pt apparently tends to reduce its bulk modulus. Relative to each other, the twenty B_0 's show no clear trend. The most energetically favorable PtN phase, B17, has 42 GPa higher bulk modulus than the proposed PtN(B3).

As we mentioned somewhere else^{67} , B_0 is far more sensitive to any change in volume than the change in E_{coh} . The case of $\operatorname{PtN}(\operatorname{B2})$ is a clear example, in which the slight decrease in V_0 overcomes the significant increase in

 $E_{\rm coh}$ leading only to a very small decrease in B_0 (Fig. 4 and Table I).

Given that all the considered phases have higher $E_{\rm coh}$ than Pt(A1), the foregoing argument fails to explain the decrease in B_0 in the case of the structures which have lower V_0 than their parent Pt(A1) and have lower $E_{\rm coh}$ than the extreme case PtN(B2). However, if one replaces V_0 in the argument above with $V_0^{\rm Pt}$, the contradiction can be lifted. Therefore, we believe that the mechanical properties in these nitrides may be dominated by the effect of the Pt-Pt bond length more than the simple number density.

Although the GGA calculated B_0 values in the present and previous works (Table I) are far smaller than the reported experimental value, our obtained bulk modulus for $PtN_2(C1)$ is 20 GPa higher than that of Pt(A1). This is exactly the measured value for Pt after the PtN formation took place. The observation was considered by Gregoryanz et al. as an indication that some N is dissolved in Pt^1 . Recalling that the B_0 of the produced platinum nitride is ~ 100 GPa than that of $Pt(A1)^1$, our GGA-obtained B_0 for $PtN_2(C1)$ is ~ 80 GPa less than the experimental value⁶⁸.

It may be worth to notice from Table I that the lattice parameter a of $PtN_2(C1)$ is 0.13 Å higher than that of PtN(B3); yet the B_0 of the former is ~ 70 GPa higher than the latter. This difference in B_0 can be attributed to the fact that in B3, N atoms occupy only half of the tetrahedral interstitial sites of the Pt sub-lattice, while in C1, the four remaining tetrahedral interstitial sites are filled with N atoms^{8,9,69}. This filling significantly reduces the compressibility but slightly increases the volume of the unit cell. This fact can also be seen readily as a consequence of the difference in the average volume per atom in the two cases (Table I).

The pressure derivative of the bulk modulus, B'_0 , measures the sensitivity of B_0 to any external pressure. The top subfigure in Fig. 4 reveals that the bulk moduli of $Pt_3N(Fe_3N)$ and $PtN_2(C2, C18 \text{ and } CoSb_2)$ increase upon application of external pressure. $Pt_3N(D0_2)$ is very sensitive and its B_0 will increase significantly under an infinitesimal excess of pressure. $Pt_3N(L1_2 \text{ and } RhF_3)$ tend to be inert; while $Pt_3N(D0_3, A15 \text{ and } D0_9)$, $PtN_2(C1)$ and all PtN phases tend to decrease their bulk modulus upon application of external pressure. Although B'_0 is a measurable quantity 55 , we couldn't find any experimental value to test our obtained values against.

D. Formation Energies

From Fig. 4 and Table I, it is evident that formation energy E_f has the same trend as the cohesive energy $E_{\rm coh}$. If E_f is taken as a measure of synthesized, then the relatively most favorable Pt₃N phases have the same synthesized as the most favorable PtN and PtN₂.

A positive value of E_f means, in principle, that, at the

temperature and pressure at which E_f is calculated, the phase is thermodynamically unstable (endothermic) and have a tendency to decompose into its constituent components. In our case, this observation is corroborated by the experimental fact that the synthesis of the platinum nitrides was achieved only at high temperature and temperature 6,60 .

Using different methods, other researchers 4,6,60 also obtained positive (zero-pressure and zero-temperature) formation energies for some PtN and/or PtN₂ phases. Some of their values are included in Table I with indication to the methods of calculations.

The obtained relative difference in E_f for $PtN_2(C1)$ and $PtN_2(C2)$ is in good agreement with Ref. 4. However, the differences in our and their obtained E_f values can be attributed to three factors: First, the difference in the obtained lattice parameter (see Table I). Second, the value of our calculated equilibrium free parameter u is 0.417 while Ref. 4 obtained 0.415⁷⁰. Third, and the most significant source of difference, the experimental value of $E_{coh}(N_2^{gas})$ in Eq. 7 was used by Ref. 4, while we calculated it as described in sub-section II D.

It may be worth mentioning here that a negative theoretical value of $E_f = -0.4 \text{ eV/atom}$ was obtained for $\text{PtN}_2(\text{C2})$ at P = 50 GPa, showing excellent agreement with experiment⁴. Moreover, Young et al.⁶ claimed that PtN_2 dissociates upon mild heating below P = 10 GPa.

E. Electronic Properties

The DFT obtained band diagrams $\epsilon_i^{\sigma}(\mathbf{k})$ and spin-projected total and partial density of states (DOS) of the most stable modifications: $\text{Pt}_3\text{N}(\text{RhF}_3)$, PtN(B3 and B17), and $\text{PtN}_2(\text{C18})$ are displayed in Figs. 6, 7, 8 and 9, respectively. Spin-projected total density of states (TDOS) are shown in sub-figure (b) in each case. Because in these four considered cases electrons occupy the spin-up and the spin-down bands equally, it was sufficient only to display spin-up DOS and spin-up band diagrams. Displaying the energy bands along densely sampled high-symmetry strings of **k**-points allows us to extract information about the electronic structure of these phases. Moreover, to investigate the details of the orbital character of the bands, the Pt(s,p,d) and N(s,p) resolved DOS's are plotted at the same energy scale.

With The Fermi surface crossing the partly occupied bands. it is clear from Figs. 6, 7, and 8 that $Pt_3N(RhF_3)$ PtN(B3) and PtN(B17) are metals.

The TDOS of Fig. 9(b) reveal that $PtN_2(C18)$ is a semiconductor with (Fig. 9(a)) its valence band maximum (VBM) at $(Y, -0.091 \ eV)$ and its conduction band minimum (CBM) at $(Y, 0.044 \ eV)$, resulting in a narrow direct energy band gap $E_g = 0.135 \ eV$ of width. Below this fundamental gap there are three bands: the deep one at $\sim -20.5 \ eV$ consists mainly of the N(2s) states. Its high DOS and sharp feature correspond to its little and slow energy variation in the **k**-space. The second band

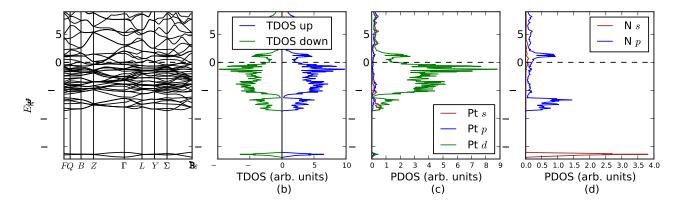


FIG. 6. (Color online.) DFT calculated electronic structure for Pt_3N in the RhF_3 structure: (a) band structure along the high-symmetry **k**-points which are labeled according to Ref. [71]. Their coordinates w.r.t. the reciprocal lattice basis vectors are: F(0.5, 0.5, 0.0), Q(0.375, 0.625, 0.0), B(0.5, 0.75, 0.25), Z(0.5, 0.5, 0.5), $\Gamma(0.0, 0.0, 0.0)$, L(0.0, 0.5, 0.0), Y(0.25, 0.5, -.25), $\Sigma(0.0, 0.5, -.5)$; (b) spin-projected total density of states (TDOS); (c) partial density of states (PDOS) of Pt(s, p, d) orbitals in Pt_3N ; and (d) PDOS of N(s, p) orbitals in Pt_3N .

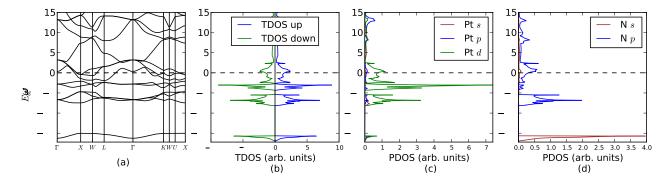


FIG. 7. (Color online.) DFT calculated electronic structure for PtN in the B3 structure: (a) band structure along the high-symmetry **k**-points which are labeled according to Ref. [71] ^a. Their coordinates w.r.t. the reciprocal lattice basis vectors are: $\Gamma(0.0, 0.0, 0.0)$, X(0.0, 0.5, 0.0), W(0.75, 0.25, 0.5), L(0.5, 0.5, 0.5), L(0.5, 0.5, 0.5), L(0.750, 0.375, 0.375), L(0.625, 0.250, 0.625); (b) spin-projected total density of states (TDOS); (c) partial density of states (PDOS) of Pt(s, p, d) orbitals in PtN; and (d) PDOS of N(s, p) orbitals in PtN.

^a The coordinates of the W point is not as the same as in Ref. [71], but they are equivalent. Also, the coordinates of U and K are not given in Ref. [71]. The coordinates of U, K and the equivalent W were created by means of XCrySDen!

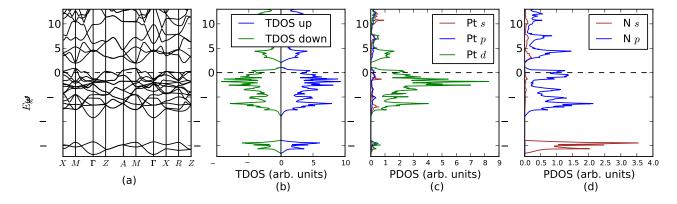


FIG. 8. (Color online.) DFT calculated electronic structure for PtN in the B17 structure: (a) band structure along the high-symmetry **k**-points which are labeled according to Ref. [71]. Their coordinates w.r.t. the reciprocal lattice basis vectors are: $X(0.0, 0.5, 0.0), M(0.5, 0.5, 0.0), \Gamma(0.0, 0.0, 0.0), Z(0.0, 0.0, 0.5), A(0.5, 0.5, 0.5), R(0.0, 0.5, 0.5);$ (b) spin-projected total density of states (TDOS); (c) partial density of states (PDOS) of P(s, p, d) orbitals in PtN; and (d) PDOS of P(s, p) orbitals in PtN.

is relatively narrow ($\sim 2.2~eV$ of width) with low density and steming mainly from a mixture of the N states with Pt(d) states. The superposition Pt(d) and N(p) states in the region from -10.314~eV to -0.091~eV below the fundamental gap constitutes the third band with highly structured, intense and narrow series of peaks. Our obtained TDOS and PDOS show excellent agreement with Ref. 60 where also $PtN_2(C18)$ was predicted to be a semiconductor, but band diagrams and E_g value are not given.

It may be worth mentioning here that $PtN(B1)^{10}$ and $PtN(B4)^{59}$ were found to be metallic, $PtN_2(C1)$ was found to be a poor metal⁸, $PtN_2(CoSb_2)^{60}$ was found to be a semiconductor, and an indirect band gap between $1.2 \ eV^{60}$ and $1.5 \ eV^{6}$ has been obtained for $PtN_2(C2)$.

F. Optical Properties

GW calculations were carried out for the PtN(B3) and PtN(B17) metallic phases at their equilibrium. Figs. 10 and 11 display the obtained real and imaginary parts of the frequency-dependent dielectric function $\varepsilon_{\text{RPA}}(\omega)$ of these two phases and the corresponding derived optical spectra (Eqs. 12-15). In each sub-figure, the optical region [$\sim (3.183-1.655)~eV \equiv (390-750)~nm$] is shaded.

The non-vanishing absorption coefficient $\alpha\left(\omega\right)$ in the whole range for both phases confirms their metallic character. As it should be the case, refraction $n(\omega)$ and extinction $\kappa(\omega)$ coefficients behave as the real $\varepsilon_{\rm re}(\omega)$ and the imaginary $\varepsilon_{\rm im}(\omega)$ dielectric functions, respectively.

As one can see from sub-figure 10(d), close to the edge of the optical region at $\sim (1.762~eV=703.768~nm)$ PtN(B3) is 50% reflector and 50% transmitter. From $\sim (2.071~eV=598.579~nm)$ to the UV region, PtN(B3) is only $\sim 40\%$ reflecting but $\sim 60\%$ transmitting. However, more of the transmitted portion in this region will be absorbed as the photon energy increases. This fact can be readily noticed if one compares sub-figures 10(c) and 10(d).

PtN(B17), as can be seen from sub-figure 11(d), is a very good reflector in the whole region until $\sim (3.000~eV=413.281~nm)$ where it equally reflects and transmits the violet light. However, less of the transmitted portion in the optical region will be absorbed as the photon wavelength decreases. This fact can be readily observed in sub-figures 11(c).

According to the best of our knowledge, there is no available experimental optical spectra for the platinum nitride. However, from their visual appearance, all the synthesized platinum nitride samples look very shiny and darker than their parent platinum in reflected light and totally opaque in transmitted light. These features suggest that PtN is either a poor metal or a semiconductor with a small band gap¹.

From Figs. 11 and 8, the above mentioned properties

are strongly met by PtN(B17), but purely seen (Figs. 10 and 7) in PtN(B3), as discussed above. Unfortunately, we did not carry out optical calculations for $PtN_2(C1 \text{ or } C2)$.

G. PtN versus PtN₂

Using our own obtained results in the present work as well as the findings of other researchers, below we make a comparison between the PtN modifications (supported by the experimentalists) and the PtN₂ phases (supported by the theoreticians):

- Given that GGA calculated lattice parameters are usually overestimated^{72–74}, the obtained values of the *a* lattice parameter for PtN₂(C1 and C2) are the closest ones to the experimental value (to within 3 % and 2 %, respectively), while the PtN phases are in poor agreement with experiment, as can be seen in Table I.
- First-principles studies of transition metals nitrides show that the B_0 's of the elemental metals are generally enhanced by nitridation^{1,75}. Compared to experiment, Table I and Fig. 4 reveal that this trend is met by $PtN_2(C1)$, while PtN(B3) has 50 GPa lower than Pt(A1).
- Like the first synthesized sample and the proposed PtN(B3) modification¹, PtN₂(C1⁸ and C2⁴) have fcc sub-lattice of Pt.
- $PtN_2(C1^8, C2^{6,60}, C18^{60})$ and $CoSb_2^{60})$ have all been found to be elastically stable, while $PtN(B3^{5,6,8,10})$ and $B17^{10})$ were found to be elastically unstable.
- Formation and cohesive energies of PtN₂(C2, C18 and CoSb₂) are lower than that of PtN(B3) [Table I and Fig. 4].
- In excellent agreement with experiment, the calculated formation energy of $PtN_2(C2)$ at P = 50 GPa was calculated to be negative⁴, while calculations found PtN(B3) to be thermodynamically unstable at all pressures⁹.
- The experimentally obtained Raman spectrum of the reproduced platinum nitride⁴ matches closely that of pyrite (FeS2), i.e. in the C2 structure, but does not match the PtN(B3) spectrum that expected from group theory⁴.
- The theoretically calculated^{6,60} Raman spectrum for PtN₂(C2) shows good agreement with the first experimentally obtained one¹.
- In agreement with the experimental observation and the visual appearance of the first produced platinum nitrides¹, PtN₂(C1) was found to be a

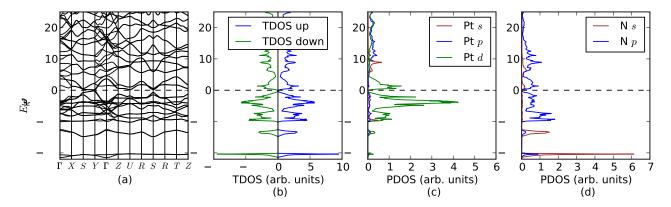


FIG. 9. (Color online.) DFT calculated electronic structure for PtN_2 in the C18 structure: (a) band structure along the high-symmetry **k**-points which are labeled according to Ref. [71]. Their coordinates w.r.t. the reciprocal lattice basis vectors are: $\Gamma(0.0, 0.0, 0.0), X(0.0, 0.5, 0.0), S(-0.5, 0.0), Y(-0.5, 0.0, 0.0), Z(0.0, 0.0, 0.0), U(0.0, 0.5, 0.0), R(-0.5, 0.5, 0.0), T(-0.5, 0.0, 0.0);$ (b) spin-projected total density of states (TDOS); (c) partial density of states (PDOS) of Pt(s, p, d) orbitals in PtN_2 ; and (d) PDOS of N(s, p) orbitals in PtN_2 .

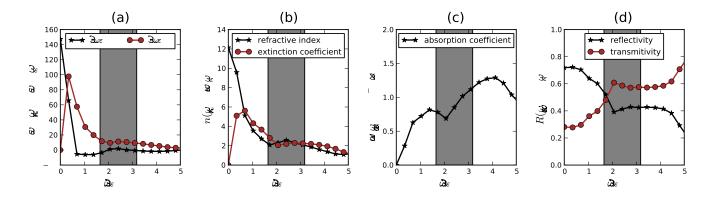


FIG. 10. (Color online.) The GW calculated frequency-dependent optical spectra of PtN(B3): (a) the real $\varepsilon_{re}(\omega)$ and the imaginary $\varepsilon_{im}(\omega)$ parts of the dielectric function $\varepsilon_{RPA}(\omega)$; (b) refraction $n(\omega)$ and extinction $\kappa(\omega)$ coefficients; (c) absorption coefficient $\alpha(\omega)$; and (d) reflectivity $R(\omega)$ and transmitivity $T(\omega)$. The shaded window highlights the optical region.

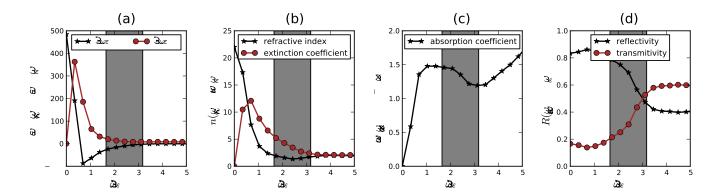


FIG. 11. (Color online.) The GW calculated frequency-dependent optical spectra of PtN(B17): (a) the real $\varepsilon_{\rm re}(\omega)$ and the imaginary $\varepsilon_{\rm im}(\omega)$ parts of the dielectric function $\varepsilon_{\rm RPA}(\omega)$; (b) refraction $n(\omega)$ and extinction $\kappa(\omega)$ coefficients; (c) absorption coefficient $\alpha(\omega)$; and (d) reflectivity $R(\omega)$ and transmitivity $T(\omega)$. The shaded window highlights the optical region.

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poor metal⁸, and we found $PtN_2(C18)$ to be a semiconductor with a small band gap.

Hence, in contrast to the proposed PtN modifications, PtN₂ phases possess many similar properties as the synthe sized phase 76 .

CONCLUSIONS

In summary, we presented a systematic series of firstprinciples calculations of the energy-optimized geometries, phase stabilities and electronic and optical properties of bulk Pt₃N, PtN and PtN₂ in twenty different crystal structures. Comprehensive comparison with experiment and with previous calculations has been made, and excellent agreement has been achieved. We found that both the lowest energy and the highest bulk modulus phases belong to the PtN₂ series and not to the PtN family. Moreover, the calculated electronic and optical properties of the PtN₂ phases show stronger consistency with experiment than the claimed PtN(B3) phase. In

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the present work, we have investigated a wider parameter sub-space than previous calculations, and to the best of our knowledge, the present work is the first to propose and to study the physical properties of Pt₃N, as well as the first to theoretically calculate the optical spectra of this new material. However, optical properties of PtN₂(C1 and C2) have not been investigated, and we strongly recommend optical calculations for these phases and obtained results should be tested against experiment. Moreover, experimentalists should provide the community with more data.

ACKNOWLEDGMENTS

We thank the CHPC for providing the supercomputer facilities to perform the GW calculations. Suleiman would like to acknowledge the support he received from Wits, DAAD, AIMS, SUST, and the ASESMA and the KWAMS13 groups.

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